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Angular Histograms: Frequency-Based Visualizations for Large, High Dimensional Data

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Abstract—Parallel coordinates are a popular and well-known multivariate data visualization technique. However, one of their inherent limitations has to do with the rendering of very large data sets. This often causes an overplotting problem and the goal of the visual information seeking mantra is hampered because of a cluttered overview and non-interactive update rates. In this paper, we propose two novel solutions, namely, angular histograms and attribute curves. These techniques are frequency-based approaches to large, high-dimensional data visualization. They are able to convey both the density of underlying polylines and their slopes. Angular histogram and attribute curves offer an intuitive way for the user to explore the clustering, linear correlations and outliers in large data sets without the over-plotting and clutter associated with traditional parallel coordinates. We demonstrate the results on a wide variety of data sets including real-world, high-dimensional biological data. Finally, we compare our methods with the other popular frequency-based algorithms.

Index Terms—Parallel Coordinates, Angular Histogram, Attribute Curves

1 INTRODUCTION

Parallel coordinates, introduced by Inselberg and Dimsdale [13, 14], is a widely used visualization technique for exploring large, multidimensional data sets. It is powerful in revealing a wide range of data characteristics such as different data distributions and functional dependencies [17]. However, one of the limitations with parallel coordinates is the clutter problem caused by rendering more polylines than available pixels. Overlapped lines often obscure the underlying patterns of the data, especially in areas with high data density.

Ben Shneiderman [22] proposed the visual information seeking mantra: overview first, zoom and filter and details on demand, as visual design guidelines for interactive information visualization application. However, this knowledge discovery process is hampered when rendering large data sets, because large data sets often cause a cluttered visualization which can obscure the overview of the data. If the user is unable to get a clear overview, it may become infeasible for them to determine which parts of the data can be filtered or zoomed in for more detail. In addition, a large data set slows interaction, making the data exploration process laborious. Therefore how to efficiently generate an information-rich overview of large data sets and enable a fast interaction process is important for information visualization design.

A straightforward solution is to reduce the number of items to be displayed and present an abstraction of the data set. For the visual analysis to remain accurate, the graphical aggregation must preserve the significant features present in the original data. Up until now, there are many frequency-based approaches proposed for clutter reduction in parallel coordinates. As one of the most widely used methods [2, 18, 20, 27], histograms are able to depict the data distribution through a binning process. However, the traditional histogram only presents univariate data. For example, a single histogram can either represent the frequency of the data plots along every vertical axis [11, 27] or the angle of line-segments between pair of axes [4], but not both at the same time.

In this paper, we present angular histograms and attribute curves.
Fig. 2. This figure shows (top) the original parallel coordinates. For each axis, three uniform bins or intervals are divided and depicted by different colors (red, blue and green); (middle) the two types of bin maps, with data frequency represented by the value displayed in each bin; (bottom) the two types of histograms. For the point-based histogram on the left, the data frequency is mapped to the length of the histogram bar. However, for the line-based histogram on the right, the frequency information is depicted by the alpha value of the histogram [20].

These techniques consider each polyline-axis intersection as a vector. We visualize both the magnitude and direction of these vectors to demonstrate the principle trends of the data. Users can dynamically interact with the plot to investigate and explore additional patterns. We evaluate our methods on real-world animal tracking data sets and perform a comparison with the traditional alpha blending [25, 26] and line-based binning algorithms [20].

The rest of the paper is organized as follows: In Section 2, we review the previous work on clutter reduction in parallel coordinates. In Section 3, we present the algorithms for angular histograms and attribute curves. In Section 4, we demonstrate interaction design including angular filtering, selection and brushing. In Section 5, we present some uses cases with respect to cluster analysis, linear correlation detection and outliers analysis. In Section 6, we discuss the performance of our visualizations. Section 7 wraps up with conclusions.

2 RELATED WORK

As a compact visual representation, parallel coordinates displays an n-dimensional data tuple as one polyline intersecting parallel axes of each data dimension. Similar to some other information visualizations [5, 6, 17, 24, 28], parallel coordinates suffers from visual clutter caused by large data sets rendered on limited screen space. This drawback hampers the further data analysis, such as investigating correlation and clusters. In this section, we mainly concentrate on previous work on parallel coordinates for large data sets. Generally, the clutter reduction methods on large data sets can be categorized as: alpha-blending, clustering, focus+context and frequency and density plots. We provide a brief overview of the literature on these methods.

Alpha Blending: Edward J. Wegman [25, 26] represented the density of the plots with transparency. In his method the sparse parts of the dataset fade away while the more dense areas are emphasised. This works well with small datasets, however, with large datasets the range of the data is much greater and consequently it is more difficult to fully represent the fidelity of complex datasets. It is difficult to obtain a clear understanding of patterns and clusters. Also, outliers may get lost.

Clustering: Fua et al. define large data sets as containing $10^6$ - $10^9$ data elements or more [8]. They adopt Birch’s hierarchical clustering algorithm which builds a tree of nested clusters of lines based on proximity information. Proximity-based coloring was introduced to demonstrate clusters, and transparency to show the mean and the extent of each cluster. Then multi-resolution views of the data can be rendered. In addition to hierarchical clustering, partitioning clustering, such as the K-means algorithm is also widely used. Johansson et al. [15] transform each K-means-derived cluster into three high precision textures, namely an animation, outliers and structure texture, and combine them into a polygon. Transfer functions are provided to highlight different aspects of the clusters.

Focus+Context: Ellis et al. propose a focus+context viewing by the use of auto sampling and a sampling lens on parallel coordinates [7]. They investigate three ways to calculate the degree of occlusion from overlapping polylines and describe a raster algorithm as the most efficient metric. The sampling rate can then be automatically determined by the measure of clutter. Novotny and Hauser develop another focus+context visualization using binned parallel coordinates [20]. The binned parallel coordinates are used for context views and the traditional polyline-based parallel coordinates are used for focus views. However, for the binned parallel coordinates, the uniform, equal-sized histogram bins may not allow for finer-resolution views of the data.

Frequency and density plots: One of the ways to reduce the clutter in parallel coordinates is based on data frequency. With this approach, the data is often aggregated and filtered by the binning process [1, 2, 3, 16, 20]. In general, binning is the process of computing the number of values falling in a given interval or bin and storing them in a bin map. The data frequency can then be visually represented by the histogram. In parallel coordinates, the bin map can either be line-segment based which stores the frequency of the line segments connecting the adjacent axes, or point based which stores the frequency of the data points along each axis, as shown in Figure 2. Much previous work adopts the bin maps which yields the line-based histograms [2, 20, 21]. They are effective at revealing clusters and outliers while further interaction support is needed to help the user select and brush the interesting data and explore the useful information.

We find that the one-dimensional point-based histogram is effective in revealing an overview of the data [11, 27], but such a histogram fails to depict the relations between the data axes. In this paper, we extend the point-based histogram to a vector-based approach. We use the histograms as the visual aggregation of both the frequency and the direction of the polyline-axis intersections. It offers the user an information-rich overview of the data. By introducing the angular information from the polyline-axis intersections, our angular histograms and attribute curves are able to depict the relationship across the data attributes. The user is able to interact with the visualization through brushing and filtering, to further explore and analyse the data. We compared our result with the line-based [20] histogram.

3 FUNDAMENTALS

Our angular histogram and attribute curves are based on a vector-based binning approach. Through their utilization they provide the user with a rich overview of the underlying data and a better understanding of the data that cannot be gained from a traditional point-based histogram view. The use of the vector-based binning approach affords several advantages: First, it requires lower space complexity ($O(n)$) compared with the line-based approach ($O(n^2)$), where $n$ represents the number of bins divided on each axis [20]. Second, it reveals the relationship of the plots between neighboring axes. Third, users can interact with the visualization by selection and brushing for further visual analysis.

In this section, we use real world animal tracking data for some of our demonstrations [9]. Biologists at Swansea university have collected large amounts of data relating to animal movement by attaching sensors to individual subjects. The data here was captured at 8Hz for 8 hours and 40 minutes. In this paper, we select 10 important data attributes which result in 1,048,566 records. The data attributes include:
two accelerometers attached on the animal recording the acceleration parameters in X, Y and Z directions and an environment sensor recording the temperature, light-intensity (Infra depth) and pressure from the outside environment. This data set can be plotted using traditional parallel coordinates, but suffers from heavy overplotting, as shown in the top of Figure 5.

3.1 Vector-Based Binning

The standard histogram is widely used for estimating data frequency and density. It classifies the data into uniform, equal-sized intervals. Each bin is assigned an occupancy value according to the number of data items belonging to it. From the perspective of visualization, the histogram is a visual abstraction that aggregates the univariate data, where the height of the histogram bar is mapped to only one variable or feature. However, displaying only one of these features is hard to represent a complete overview of the data. If we map the slope of each line segment to a direction, then the polyline segment-axis intersections can be treated as unit vectors, as shown in Figure 3. In order to visualize the vector aggregations, at least two features, namely direction and magnitude, have to be encoded at the same time. We utilize two parallel bins on each vector with one bin recording the direction information and the other the frequency.

3.2 Angular Histograms

The standard point-based histograms are initially rendered in the second row of Figure 5. The height of each histogram bar is mapped to data frequency. From this visualization, we are able to discern the scalar distribution along each axis. However, this histogram representation lacks the angular information from polylines intersecting each dimensional axis. Thus we cannot discern and infer the relationships between the neighboring data attributes.

In Section 3.1, we introduced vector-based binning. The magnitude and direction of the vectors along each axis of the parallel coordinates are aggregated. Here we propose the angular histogram as an extension to the standard. The basic idea is that for each histogram we calculate the mean angle of the vectors and rotate the histogram bars by this angle. Then again the histogram bars can be considered as a vector, with length equal to the data frequency and the direction as the average angle of all its underlying polyline segment-axis intersections, as shown in the third row of Figure 5.

Different histogram bars on the same axis might overlap when rotate by an certain angle. We can apply alpha blending and silhouettes on the histogram bars to overcome the overlapping problem, as shown in Figure 4.

Although the angular histogram is able to convey the vector distribution, it still suffers from some drawbacks. The end points and the width of histogram bars determine the overall profile of the original, underlying line-segment distribution curve. Too large or too small of a bin width can cause undersmoothing or oversmoothing. A common statistical method for smoothing a data distribution, such as KDE (kernel density estimation), GMM (Gaussian mixture model) suffers from the computational complexity (particularly in high-dimension spaces) and the dependence on a bandwidth parameter or initial number of clusters[23]. With this in mind, we have decided to leave the bin width as a user option. The user is able to interactively select the number of bins in each axis and obtain the corresponding angular histograms both locally and globally. Global bin selection applies the bin width to all
histograms across all axes. Whereas local bin selection allows the user adaptively select the bin size in different areas. For example, the areas with high data density might require smaller bin width and thus more bins to depict finer detail.

Due to their frequency-based nature, histogram bins with relatively low density can be difficult to detect. One way to address this problem is to use a logarithmic histogram as shown in the fourth row of the Figure 5. The corresponding logarithmic angular histogram is rendered in the fifth row of Figure 5. From this visualization, low-frequency histogram bars and their directions are preserved.

When the histogram bars are rotated by a given angle, it’s more difficult to discern and compare their relative lengths. It often happens that a given large data set is not balanced and highly skewed. To address this problem, we can apply color mapping on the histogram bars to represent the data density. In order to enable smooth transitions between the angular histogram bars, the frequency curve which connects the center point of all histograms is rendered, as shown in the top of Figure 1.

3.3 Divided Angular Histogram

In the previous sections we introduced the angular histogram where the direction of each histogram bar is represented by the average angle. Although the mean value is a representation of the central tendency, it can be sensitive to extreme values (e.g., outliers) and the standard deviation might become significant.

In order to accurately display the profile of the data trend, we propose the divided angular histogram as one of our user options. On the left of first row in Figure 6, we observe that there are two data trends passing through a histogram bin, pointing upward and downward respectively to the neighboring axis. If we calculate the average angle of these vectors, their positive and negative slopes cancel each other and lead to a flat histogram angle. In order to truthfully depict the data trend, we split the histogram bin into two separate groups: one contains vectors with an upward slope, such as $b$ in Figure 3. The other contains vectors with a downward slope, such as $a$ in Figure 3. For each bin, we quantify the frequency of the upward and downward vectors, which can be denoted by $n$ and $m$ respectively. We also calculate the average angle for upward and downward vectors, which can be denoted by $\bar{\beta}$ and $\bar{\alpha}$, as shown in the right of the first row in Figure 6.

In this figure we are able to see the original histogram bar is divided into two separate groups with one pointing upward and the other downward.

Because the splitting process increases the number of histogram bars displayed on the screen and might introduce clutter, we choose to split only a certain number of histogram bars to reveal the major data trend with more accuracy while avoiding the clutter problem. We still use the average angle to represent the undivided histograms’ directions. Two user-centered approaches are provided to specify the number of histograms to be divided. The first approach enables the user to directly select and split any histogram bars they are interested in. The second approach defines a condition in order to automatically filter out undivided histograms. The condition can be expressed as: if the difference between the number of upward and downward vectors is small and the angle between the upward and downward vectors is large in a histogram bin, then this histogram bar is divided. This condition can be formulated as follows:

$$0.5 - \xi < \frac{n}{n+m} < 0.5 + \xi \quad \land \quad (|\bar{\alpha}| + |\bar{\beta}| > T)$$

where $\xi$ represents a small value and is in the range $[0,0.5]$. In our case, we set $\xi$ to 0.2 to ensure the number of upward and downward vectors are close. $T$ represents a threshold value and is in the range $[0,180^\circ]$. In our case, we set $T$ to $80^\circ$.

To offset the effect on average angle caused by a small number of outliers, we can use the trimmed mean [10] only if either the number of upward or downward vectors dominates in a histogram bin, otherwise the histogram angle remains unchanged. This can be defined as:

$$\theta_{\text{NEW}} = \begin{cases} 
\bar{\beta} & \text{if } \frac{n}{n+m} > 0.9 \\
\bar{\alpha} & \text{if } \frac{n}{n+m} < 0.1 \\
\theta_{\text{OLD}} & \text{otherwise}
\end{cases}$$
where $\theta_{EW}$ is the updated histogram angle and $\theta_{OLD}$ is the original histogram angle. We choose a small threshold to avoid trimming too large a portion which may lose valuable information [10].

After the histogram splitting and trimmed mean, the angle deviation can be reduced compared to the original angular histogram as shown in the second and third row of Figure 6. We can also obtain a more accurate cluster profile when following the direction of the histogram bars. The divided angular histogram works well in different orderings of our animal tracking data set, as shown in Figure 7. Besides providing a default setting for $\xi$ and $T$, we also offer interaction support for the user to customize these parameters to explore the total solution space. The limitation of the divided angular histogram lies in its inability to split the vectors with same direction, such as a histogram bin that only contains upward or downward vectors. But we can further convey the standard deviation of histogram angles to the user, as discussed in Section 5.

### 3.4 Attribute Curves

Sometimes even the logarithmic histogram cannot depict outliers with very low frequency. The top of Figure 9 shows the daily total volume, open price, close price, the highest and lowest value of transaction in NASDAQ stock market during 1970 and 2010 [12]. Most data is gathered on the lower part of the axes and suffer from clutter. From the original parallel coordinates we observe there are few high volumes and values of transactions on the upper half of the axes. These values are not preserved in the logarithmic angular histograms shown in the middle of Figure 9, because some low-frequency histogram bins suffer from the low resolution of the display space and visually they just look the same as empty bins. Thus the angular histograms incorrectly inform the user that no data exists in the upper half of the axes. In this section, we propose a user option called attribute curves to depict such outliers. In contrast to the discrete nature of angular histograms, attribute curves convey a smooth distribution of the underlying polyline data based on the angular frequency of the underlying polylines-axis intersections. The attribute curves are able to preserve the extreme values or outliers and indicate empty bins along the axis. In addition, they reveal the data distribution without the clutter associated with traditional parallel coordinate plots. In attribute curves, the bin size used to compute angular-frequency is the same used for vector-based binning. Vector-based binning stores vector direction in the bin size used to compute angular-frequency is the same used for웠가 바야 최대값, attribute curves are able to preserve the few outliers on the top and indicate that these outliers have a large angle. Because we are using the absolute histogram angle in equation (3), our attribute curves will not suffer from the problem that the positive slope and negative slope may cancel each other, as discussed in Section 3.3. The absolute angle indicates the change rate in the data plot. A large angle often suggests a dramatic change of the data plot in a histogram bin from one axis to the next, while a small angle suggests a lack of change in the data plot between adjacent axes. For a better demonstration the middle part of the fourth axis in the bottom row of Figure 9 is brushed. We observe a steady transition of the data plots between the fourth and fifth axis and a relatively large change rate in the other adjacent axes from the brushed polylines. A few gaps in some part of the axes indicate the existence of empty histogram bins. From the color mapping, we are able to see a clear data distribution in the lower part of the axes which cannot be gained from the original parallel coordinates.

Attribute curves can be also applied to our animal tracking data sets, as shown in the bottom of Figure 1. By looking at the shape of the curve, we learn the relationship between the neighboring axes, and a principal data trend across attributes can be inferred from the density color coding. The user could also remove the parallel vertical axis from the attribute curves to form unparalleled coordinates. We recognize that attribute curves could pose challenges with respect to interpretation. This is true about many novel visualization techniques. It is even true about parallel coordinates. This concern was not raised by the users we have showed the visualization to so far. However
Fig. 10. This figure shows two results of the angular brushing on our histograms. The first row displays the angular histogram with the flat angle and the second row depicts the large angles.

Fig. 11. This figure shows the two ways of selection on our animal tracking data sets. The first row shows multiple selection and Or-Brush; The second row illustrates the range selection.

a full user-study is necessary to analyze interpretation. This is one of our future work directions. The algorithms we present are not intended to replace the traditional parallel coordinates visualization. They are meant as complements in order to facilitate exploration of large data sets.

4 INTERACTION

In the previous sections, we demonstrate how the angular histogram and attribute curves can be used for presentation and data overview. The next step is to allow the user drill down into the interesting parts of the data and explore the useful information. To facilitate the information seeking mantra, we provide three types of interaction support including angular filtering, selection, and brushing on our attribute curves.

4.1 Angular Filtering

The angular filtering is similar to the work in [11]. The angular brushing [11] is effective in revealing the relations between the neighboring data attributes by filtering the slopes of the line segments. However utilizing the angular brushing on the original large data sets may cause a cluttering problem and slows down the performance. Considering the angular histogram provides a visual aggregation of the vector directions, it can be filtered by the angles of the histogram bars. The user is able to define the range of histogram angles they are interested in and the histogram bars with angles in this range will be rendered. We demonstrate two brushing results in this section: one displays the angular histograms only with small angles, as shown in the top of Figure 10; the other displays the angular histograms with sharp angles, as shown in the bottom of Figure 10. The obliqueness of the angular histograms depicts the relationship of the data between the neighboring axes.

4.2 Selection

The user is able to select the histogram bars of interest and the original underlying polylines passing through the given bin will be rendered. The histogram bars can be selected in three different ways, including the singular selection, multiple selections and range selection. The singular selection enables the user select any individual histogram bar. The multiple selections allow the user select various histogram bars at the same time, as shown in the first row of Figure 11. The range selection allows the user select a range of histogram bars, such as in the upper region of the axis, as shown in the second row of Figure 11. We enable alpha-blending on the selected polylines to avoid clutter. In order to show the context, the angular histogram of the selected axis is also rendered.

4.3 Composite Brushing

The user is also able to select the angular histogram bars from different axes and perform a composite brushing, such as an AND-brush or OR-brush [11]. In the context of large data sets we find that the AND-brush is particularly useful in reducing the clutter and finding the major trend in the data. As shown in Figure 15, the angular histogram provides a context view while the focused polylines are rendered.

5 USE CASES

For demonstration, we use two different axis orderings of our animal tracking data set which cause serious clutter. In the following sections, we demonstrate our methods with respect to the performance of cluster analysis, correlation detection and outlier analysis. We compare our methods with alpha blending [25, 26] and line-based binning [20]. Our techniques rely on the user to provide numerical orderings for nominal data.

5.1 Cluster Analysis

In the previous sections we introduce the angular histogram which indicates the path where the majority of data flows across the parallel coordinates. Although the divided angular histogram could reduce the
In this section, we specifically demonstrate how our angular histograms can be used to enhance visual correlation analysis for large data. The different levels of data correlation will impose various shapes on angular histograms. In order to observe the underlying rules for analyzing such shapes, we prepare a group of large sample data sets with different correlation levels for illustration. The sample data group is manually generated according to Jing Li et. al’s work [19]. We show 6 correlation levels whose Pearson Coefficients [10] ranges from -1 to 1, as shown in the first row of Figure 14. The second row of Figure 14 shows the same data but rendered with a smaller alpha value.

The third row of Figure 14 shows the angular histograms applied to the sample data sets. We color code the sharpness of the angular histogram, from red to blue depicting the largest to smallest slope. As the correlation decreases, the angular histograms reveal a series of changing patterns. The slopes of the histogram bars are increasing, and the distribution of the downward slope points tend to cluster around the upper region of the axis and the upward slope points tend to cluster around the lower region of the axis. Compared with alpha blending, the angular histograms uncover the rate of change of the line slopes as the coefficient strength decreases: the closer the lines to the middle of the axis, the slower their slopes change and the closer to the lines to the polar ends of the axis, the faster their slope change.

5.3 Outlier Analysis

In statistics, an outlier is an observation that is numerically distant from the rest of the data. How to present the major trend in the data while preserving the outliers is an important question in visualization design. In Section 3, we briefly discussed the strength of attribute curves using the NASDAQ data set. The logarithmic histogram falls short in preserving the very low density histogram bins and the attribute curves could complement this and indicate the change rate of the data plots between adjacent axes. Therefore, these two approaches can be combined together for outlier analysis.

In this section, we specifically demonstrate how our angular histogram can enhance the outlier analysis for the traditional alpha-blending method. As shown in Figure 13, the top row is two different orderings of our animal tracking data set rendered in low alpha value (\(\alpha = 0.003\)). Although we set the opacity to a very low level, there are

\[
\alpha_c = \sqrt{\frac{1}{n-1} \sum_{i=1}^{n} (x_i - \bar{x})^2}
\]

where \(n\) is the bin count, \(x_i\) is each vector’s angles and \(\bar{x}\) is the mean angle of this bin.
still some regions suffering from the clutter problem and the low frequency area is not preserved. From the second axis in the first column, first row of the Figure 13, we observe that the majority of the data is gathered on the middle part of the axis. If the user wants to know how the low and high values in this axis correlate with the neighboring axes, then it becomes difficult to see from alpha-blending. This is also happened to the eighth axis in the second column, first row of the Figure 13. However, from the angular histogram shown in the third row of Figure 13, we are able to see the relationship between the low-frequency data and the neighboring axes. We could subsequently brush such area and the polylines passing through these histogram bins are rendered.

Fig. 16. This figure shows two outlier-preserving visualizations. The underlying cluster is rendered by line-based histogram and the outliers can be brushed using the angular histogram.

Our angular histogram could also be incorporated with the line-based histogram, as shown in Figure 16. The underlying cluster can be rendered by the line-based histogram. From the angular histogram, user is able to learn an informative overview of the data. Such overview will guide them to select and brush the interesting parts of the data, such as low-frequency histograms, on top of the principle data trend, as shown in the Figure 16.

6 Discussion

For a data set containing \( n \) dimensions and \( m \) records, with each of its attributes uniformly divided into \( k \) intervals, we need to construct \( (n-1)k^2 \) bins for storing the line frequency [20], whereas only \( 4nk \) bins for the vector frequency. The comparison of the two methods is shown in the Figure 17.

Moreover, reordering the axis in parallel coordinates generates a new bin map. From previous work [2], the way to handle reordering is to pre-compute the bin maps for all possible axis permutations. In this respect, our vector-based histogram has the advantage of taking up much less processing time and memory space than the line-based histogram.
histogram, especially for data sets with high dimensions. The line-based histogram [20] is able to present a clear representation of the principle trend in the data. However, due to the fact that it only aggregates the frequency of the lines between pair of axes, the data trend it reveals is not as coherent as our brushed polylines across all data attributes. In order to enhance the clustering and outlier effect, the line-base histogram [20] utilizes different filters, such as Gaussian or Median filters. But except changing the bin size, the user does not have much control of the visualization. Whereas in our vector-based histograms, we aim to facilitate the information seeking mantra for the user. The data overview is presented by the angular histogram. Following the direction of the high density histogram bars give a general cluster profile. The use of the logarithmic angular histogram and attribute curves depict the outliers in various levels to the user. When the user obtains a good overview, we offer various interaction supports for them to perform in-depth visual analysis. Our technique is not aiming at automatic cluster or outlier detection, instead we tend to leave the control with the user by providing an informative overview accompanied with the interaction support. The user has a high degree of freedom in determining their interested parts of the data. We compared our angular histogram with the line-based approach in Figure 7 to ensure the overview of the data is accurate and not biased.

7 CONCLUSION

In this paper, we introduce the angular histogram and attribute curves for visual analysis of large and high dimensional data. Our method is based on the vector-based binning which not only depicts the data distribution but also reveals the angular information of the polyline-axis intersections. Therefore the angular histograms and attribute curves offer an information-rich overview. Also we provide various interactions for the user to select and brush the interesting subset of the data. We compare and evaluate our methods with the line-based histograms [20] and alpha-blending with respect to cluster analysis, linear correlation detection and outlier analysis. We demonstrate our technique using the real world animal tracking data set. In the future, we plan to run a comparative user study for the evaluation of our techniques and further comparison with other techniques.

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